

EC Chemistry 1 – Test 1 – Duration: 1h

No document allowed. Any non-connected calculators allowed.

Answers must be justified.

The results will be given with the appropriate number of significant figures.

Data:

Rydberg's constant for hydrogen: $R_H = 109\,677\text{ cm}^{-1}$

Planck's constant: $h = 6,626 \times 10^{-34}\text{ J}\cdot\text{s}$

Avogadro's number: $N_A = 6,022 \times 10^{23}\text{ mol}^{-1}$

Electron mass: $m = 9.10939 \times 10^{-31}\text{ kg}$

Light speed: $c = 2.998 \times 10^8\text{ m}\cdot\text{s}^{-1}$

Elementary charge: $e = 1.602 \times 10^{-19}\text{ C}$

$E_{\text{kinetic}} = \frac{1}{2} m v^2$

I. Atomic spectrum of Hydrogen (~ 6 pts)

The emission spectrum of one of the series of the hydrogen atom is shown below. The lines of wavelengths λ_1 , λ_2 and λ_3 are those with the highest values for this series.

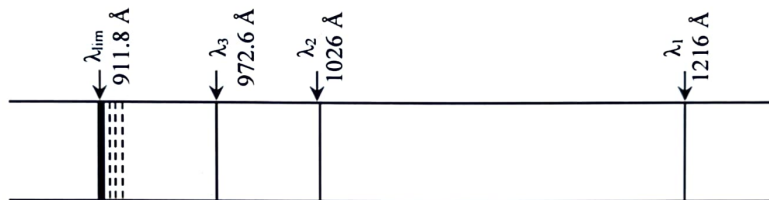


Figure 1: The emission spectrum of one of the series of the hydrogen atom

- In terms of energy, for a given series in an emission spectrum, to which transitions are associated the short wavelength and the long wavelength limit, respectively?
- Regarding the spectrum shown in Figure 1: to which domain(s) of the electromagnetic wave spectrum does this series belong to?
- Towards which level n do the transitions involved in this series take place?
- Calculate in eV the energy of this level n with the appropriate number of significant figures.
- Represent on a Grotrian diagram the transitions corresponding to λ_1 , λ_2 , λ_3 and λ_{lim} . The numerical values of all the energy levels involved in these transitions will be given (in eV, to the nearest 0.01 eV) as well as the values of the associated quantum numbers.

II. About Boron (~ 8 pts)

- The electrons of an atom are distributed in different atomic orbitals (or quantum boxes) characterized by three quantum numbers (n , ℓ , m_ℓ).
 - Name these three quantum numbers. In the general case, what values can they take?
 - For each of the (n , ℓ , m_ℓ) sets below, is there an atomic orbital that would correspond to these 3 values? If so, give the symbol of the associated **quantum subshell**.

n	ℓ	m_ℓ
3	2	-2
2	0	0
2	3	-3

- Let's consider the (stable) isotope for Boron : $^{11}_5\text{B}$
 - Specify the number of protons, neutrons and electrons for this isotope $^{11}_5\text{B}$.
 - In which subshell(s) are located the valence electrons of this atom $^{11}_5\text{B}$?
 - How many single electron(s) does this atom contain?

3. Give the notation associated with the hydrogen-like ion related to the Boron element.
4. The ionization energy E_i^Z of a hydrogen-like system relative to a chemical element which atomic number is Z expresses as :

$$E_i^Z = Z^2 \times E_i^H$$

where E_i^H represents the ionization energy for hydrogen, as far as **the Rydberg's constant for the hydrogen-like ion and for hydrogen are taken as equal**. This condition is supposed to apply in this exercise.

- a) Prove this relationship.
 - b) Calculate the energy required to extract the electron from the hydrogen-like ion associated to the Boron element. The result will be expressed in eV, J and $\text{kJ}\cdot\text{mol}^{-1}$ with the appropriate number of significant figures.
5. When this hydrogen-like ion is excited by a frequency band $\nu_{\min} < \nu < \nu_{\max}$, the resulting emitted spectrum is composed of six radiations. What is the maximum frequency ν_{\max} of the photons used?

III. Spectroscopy for hydrogen-like systems (~ 6 pts)

As the results of two experiments, a researcher gets two absorption spectra of hydrogen-like systems that are referred by the letters A and B. The wavelength of the highest energy radiation in spectrum A is equal to 101.3 \AA and that in spectrum B is equal to 25.33 \AA . The value of the Rydberg constant is identical, **but not known**, for these two hydrogen-like systems.

1. Calculate the ionization energy of the two hydrogen-like systems corresponding to the spectra A and B. The result will be expressed in $\text{kJ}\cdot\text{mol}^{-1}$ with the appropriate number of significant figures.
2. Calculate the ratio Z_B/Z_A between the atomic numbers Z_A and Z_B of the corresponding elements.
3. What condition must the ratio Z_B/Z_A satisfy for the radiation emitted by the ion of atomic number Z_B during the transition $n=4 \rightarrow n=2$ to ionize the ground state of the ion of atomic number Z_A ? Is this condition fulfilled?

End of the subject