

19/75

Ex. 1

Linear interpolation

Q. 1.1

```

public static double[][] transposeMatrix (double [][] a) {
    double [][] b = new double [a.lengtha[0].length][a.length];
    for (int i=0; i < a.length; i++) {
        for (int j=0; j < a.lengtha[i].length; j++) {
            b[j][i] = a[i][j];
        }
    }
    return b;
}

```

1

Q. 1.2

```

public static void displayMatrix (double [][] a) {
    for (int i=0; i < a.length; i++) {
        for (int j=0; j < a[i].length; j++) {
            System.out.print (a[i][j] + " ");
        }
        System.out.println();
    }
}

```

1

Q. 1.3

```
public static double[] matrixVectorProduct (double[][] a, double[] b) {
    double[] c = new double [a.length];
    for (int i=0; i < a.length; i++) {
        for (int j=0; j < a[i].length; j++) {
            c[i] = c[i] + a[i][j] * b[j];
        }
    }
    return c;
}
```

1.5

Q 1.4

```
public static double[][] matrixProduct (double[][] a, double[][] b) {
    double[][] c = new double[a.length][b[0].length];
    for (int i=0; i < a.length; i++) {
        for (int j=0; j < b.length; j++) {
            for (int k=0; k < b[j].length; k++) {
                c[i][k] = c[i][k] + a[i][j] * b[j][k];
            }
        }
    }
    return c;
}
```

Q.1

it is OK
but mathematically speaking
we prefer to write

```

Q 1.5 public static double[] solveSystem (double[] x, double[] y) {
    double[] s = new double[2];
    double[][] u = new double[x.length][2];
    for (int i=0; i < x.length; i++) {
        u[i][0] = x[i];
        u[i][1] = 1.0;
    }
    double[] s1 = new double[2];
    s1 = matrixProduct (invertMatrix (matrixProduct (transposeMatrix (u), u)),
        matrixProduct (transposeMatrix (u),
        matrixVectorProduct (transposeMatrix (u), y)));
    s[0] = s1[0];
    s[1] = s1[1];
    return s;
}

```

2.5

```

Q 1.6 public static double computeError (double[] x, double[] y, double[] s) {
    double e=0; error = 0;
    for (int i=0; i < x.length; i++) {
        error = error + (y[i] - s[0]*x[i] - s[1])*(y[i] - s[0]*x[i] - s[1]);
    }
    return error;
}

```

1.5

Q. 1.7

```
public static main String main (String args[]) {
```

```
double x = new double [6], {0.8, 2.2, 2.8, 4.2, 4.8, 6.2};
```

```
double y = new double [6], {11.9, 21.7, 31.8, 42.0, 51.9, 61.9};
```

```
double s = new double [2];
```

```
s = solveSystem (x, y);
```

```
int error = computeError (x, y, s);
```

```
System.out.println (s[0] "a=" + s[0]);
```

```
System.out.println ("b=" + s[1]);
```

```
System.out.println ("Error is " + error);
```

```
}
```

2. The return of the Binary

Q. 2.1 public class Binary {

```
public int b0;
```

```
public int b1;
```

```
public Binary (int b0, int b1) {
```

```
    this.b0 = b0;
```

```
    this.b1 = b1;
```

```
}
```

```
public Binary () {
```

```
    this.b0 = 0;
```

```
    this.b1 = 0;
```

```
}
```

```
public String toString () {
```

```
    return b1 + "" + b0;
```

```
}
```

```
// file with name Binary.class, stored in C:/Users/Catalin/Desktop/Binary
```

```
}
```

Q. 2.2

```
public class TestBinary {
    public static String main (String args[]) {
new Binary u = new Binary (1, 0);
        Binary v = new Binary (1, 1);
        System.out.println (u);
        System.out.println (v);
    }
}
```

1

// file is stored with name TestBinary.java, in C:/Users/Catekin/Desktop/Binary

}

Q. 2.3

Methods for Binary class:

```
public int toDecimal () {
    int a;
    a = b0 + 2 * b1;
    return a;
}
```

```
public intboolean isEven () {
    boolean even = false;
    if (b10 == 0) {
        even = true;
    }
    return even;
}
```

1.5

Code in main:

```
System.out.println("The decimal form is " + u.inDecimal());  
if (u.isEven() == true){  
    System.out.println(u + "The number is even");  
} else {  
    System.out.println("The number is odd");  
}
```

Q. 2.4

```
public static Binary integerToBinary(int v){  
    Binary u = new Binary();  
    u.b0 = v % 2;  
    u.b1 = (int) v / 2; double tmp = v / 2;  
    u.b1 = (int) tmp;  
    return u;  
}
```

Not the idea!

↳ a constructor

```
public Binary(int u)  
{  
}
```

no interest!

1.5

Q. 2.5

The addition of u and v are logically, by following the idea of binary and declaration of the class Binary, only if their sum together don't exceed $(11)_2$ (or $(3)_{10}$), because otherwise they'll get out of the idea of binary computation. ~~The~~

The addition with 5 is already impossible because it exceeds the representation in 2 bits.

If we still suppose that we can lose some the bits that exceed the representation in 2 bits, then we'll get a wrong answer represented in base 10.

1.5

Implementation of addInteger method if it follows the constraints

```
public addInteger  
public Binary addInteger (Binary v) {  
    v.b0 = u.b0 + v.b0;  
    v.b1 = u.b1 + u.b1;  
    return v;  
}
```

~~but still that's not possible to~~

```
public void addInteger (Binary v) {  
    v.b0 = this.b0 + v.b0;  
    v.b1 = this.b1 + v.b1;  
}
```