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Exercise 1. Fill in the blanks with the simplest equivalent. No justifications required.

$$\cos(\ln(\cos(x))) - 1 \underset{x \rightarrow 0}{\sim} \frac{-(\ln(\cos(x)))^2}{2} \underset{x \rightarrow 0}{\sim} \frac{-(\cos(x)-1)^2}{2} \underset{x \rightarrow 0}{\sim} \frac{-x^4}{8} \checkmark$$

$$\frac{e^{\cosh(x)} - e}{\sinh(x)} \underset{x \rightarrow 0}{\sim} \frac{e(e^{\cosh(x)-1} - 1)}{\sinh(x)} \underset{x \rightarrow 0}{\sim} \frac{e(\cosh(x)-1)}{\sinh(x)} \underset{x \rightarrow 0}{\sim} \frac{-ex}{2} \checkmark$$

$$\arccos(x) - \arccos(1/2) \underset{x \rightarrow 1/2}{\sim} \frac{-1}{\sqrt{1-(1/2)^2}} (x - \frac{1}{2}) \underset{x \rightarrow \frac{1}{2}}{\sim} \frac{-1}{\sqrt{3/4}} (x - \frac{1}{2}) \underset{x \rightarrow \frac{1}{2}}{\sim} \frac{-2}{\sqrt{3}} (x - \frac{1}{2}) \checkmark$$

$$\underbrace{\frac{-1}{\sqrt{1-(1/2)^2}}}_{\arccos'(1/2)}$$

Exercise 2. Fill in the blanks:

$$(1 - 2x + 3x^2 + o(x^2)) + (x - 3x^2 + o(x^3)) \underset{x \rightarrow 0}{=} 1 - x + o(x^2) \checkmark$$

$$(1 - 2x + 3x^2 + o(x^2))(x - 3x^2 + o(x^3)) \underset{x \rightarrow 0}{=} x - 3x^2 - 2x^2 + 6x^3 + 3x^3 + o(x^3)$$

$$\underset{x \rightarrow 0}{=} x - 5x^2 + 9x^3 + o(x^3)$$

$$(1 + x + \frac{x^2}{2} + o(x^2))(1 - x + \frac{x^2}{2} - \frac{x^3}{6} + o(x^3)) \underset{x \rightarrow 0}{=} 1 - x + \frac{x^2}{2} + x - x^2 + \frac{x^2}{2} + o(x^2)$$

$$\underset{x \rightarrow 0}{=} 1 + o(x^2) \checkmark$$

Exercise 3. True or false? no justifications required.

$$\cos(x^2) \underset{x \rightarrow 0}{\sim} e^x + 10x^5 \quad \text{False} \checkmark$$

$$\ln(5x) \underset{x \rightarrow +\infty}{=} o(\sqrt{x}) \quad \text{True} \checkmark$$