

Name: *DEVIN Triston 61*

11/20

12/10 = 10/10

Exercise 1. Let A be a non-empty set, let $f : A \rightarrow \mathbb{R}$ and let $M \in \mathbb{R}$. Recall the definition of " M is an upper bound of f ."

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$$\forall x \in A, (M \geq f(x))$$

Exercise 2. Let A be a non-empty subset of \mathbb{R} symmetric with respect to 0, and let $f : A \rightarrow \mathbb{R}$. Recall the definition of " f is even."

2

$$\forall x \in A, f(x) = f(-x)$$

Exercise 3. Let A and B be two non-empty subsets of \mathbb{R} symmetric with respect to 0, and let $f : A \rightarrow B$ and $g : B \rightarrow \mathbb{R}$. We assume that f is odd and that g is odd.

1. What can you say about the parity of $g \circ f$? (no justifications required, the proof will be required in the next question).

3

$g \circ f$ is *odd*

2. Prove it!

4

Let $x \in A$

$g \circ f = g(f(x))$ since f is odd $g(-f(x)) = g(f(-x))$
 so $-g(f(x)) = g(f(-x))$
 or since g is odd $-g(f(-x)) = g(f(x))$

Exercise 4. Let f be the polynomial function defined by:

$$f : \mathbb{R} \rightarrow \mathbb{R}$$

$$x \mapsto x^4 + x^3 - 3x^2 - 5x - 2$$

$$\begin{array}{r} x^4 + x^3 - 3x^2 - 5x - 2 \\ \underline{x^4 + x^3} \\ -3x^2 - 5x - 2 \\ \underline{+3x^2 + 3x} \\ -2x - 2 \end{array}$$

1. Among the numbers -1 and -2 , only one of them is a root of f (that we shall denote by x_0). Which one is it? (no justifications required).

0

$x_0 = -2$ -1 is a root

2. Find a polynomial function g such that $\forall x \in \mathbb{R}, f(x) = (x - x_0)g(x)$.

0

$$\forall x \in \mathbb{R}, g(x) = x^3 + 3x^2 + 3x + 1 \quad x^3 - 3x - 2$$