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# Physics I E

13/20 Good Work!

0.5 1) For an ideal coil  $\underline{z} = jL\omega$

0.5 For an ideal capacitor  $\underline{z} = \frac{1}{Cj\omega}$

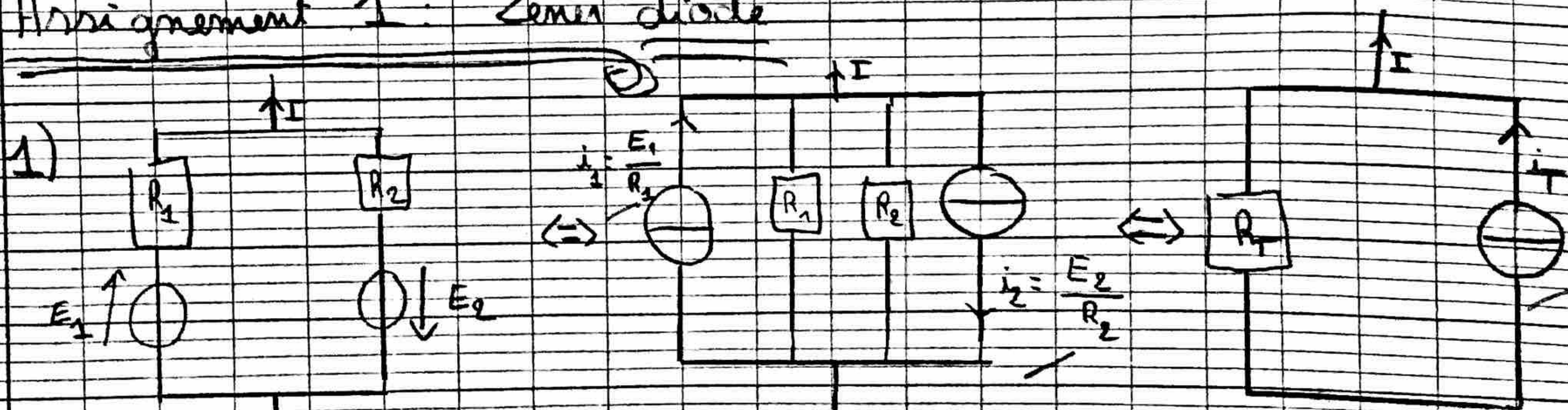
2)  $i_1(t) = 4\sqrt{2} \cos(100\pi t + \frac{\pi}{4})$

0.5 Hence  $U_{m} = 4\sqrt{2}$  we know that  $U_{pp} = 2U_{m} = 8\sqrt{2}$  (demonstration)

0.5 here  $\omega = 100\pi \text{ rad.s}^{-1}$  since  $\beta = \frac{\omega}{2\pi}$ ,  $\beta = 50\text{Hz}$   
 ( $\varphi = \frac{\pi}{4}$  rad  $T = 0,02\text{s}$ )

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## Assignment 1: "Zener diode"

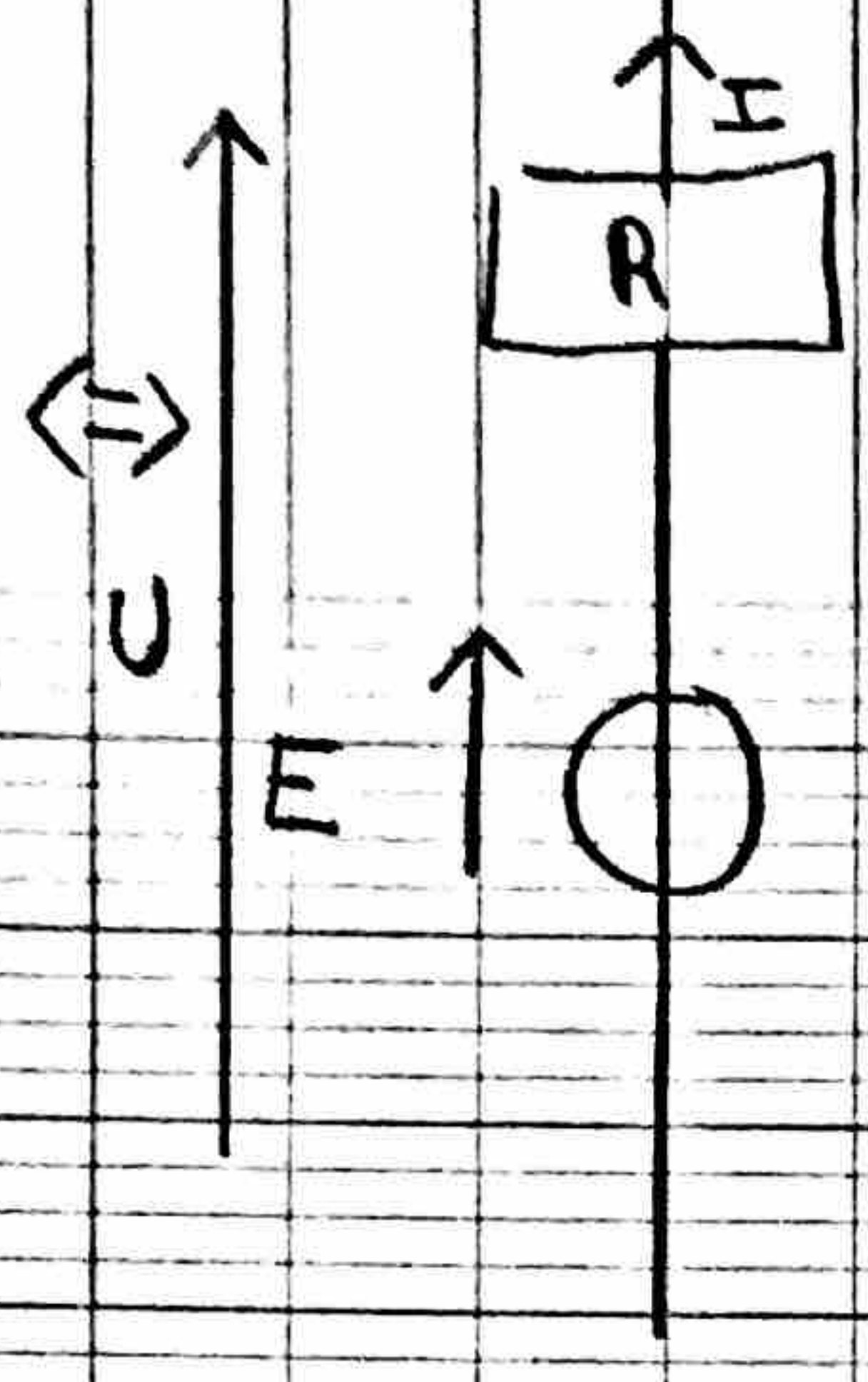


with  $R_T = \frac{R_1 R_2}{R_1 + R_2}$

$I_T = \frac{E_1}{R_1} - \frac{E_2}{R_2}$

(1)

2/2



with  $R = R_1 = \frac{R_1 \times R_2}{R_1 + R_2}$

and  $E = E_T = i_T \times R_T$

$$= \left( \frac{E_1}{R_1} - \frac{E_2}{R_2} \right) \times \frac{R_1 R_2}{R_1 + R_2}$$

$$E = \frac{E_1 R_2 - E_2 R_1}{R_1 + R_2}$$

2) In Passive sign convention (PSC)

$U = E - RI$  (see figure above for conventions.) Yes, thank!

0.5

Hence  $I = \frac{E - U}{R}$  since  $E = 1.5V$  and  $R = 50 \Omega$

$I = 0.03 - \frac{U}{50}$  Hence the I-V curve of the generator and the resistor is a straight line.

When  $U = 0V$   $I = 0.03 A = 30mA$

$U = 1V$   $I = 0.01 A = 10mA$

0.5

(cf graph appendix)

0.5

We find  $U = 0V$  and  $I = 0.03A$  as operating point.

less true since here the operating points are not calculated.

Yes, you're right

The graphical method implies a lot of uncertainties especially since here the I-V curve of the diode is thick?

3) If now the terminal of the diode are switched we still have the same I-V curve for the generator and the resistor but the diode one is not the same anymore.

We know now that if  $i < 0$   $u = 0$  Excellent!  
and if  $i > 0$   $u = 1$

0.75

(cf graph appendix 2).

0.25

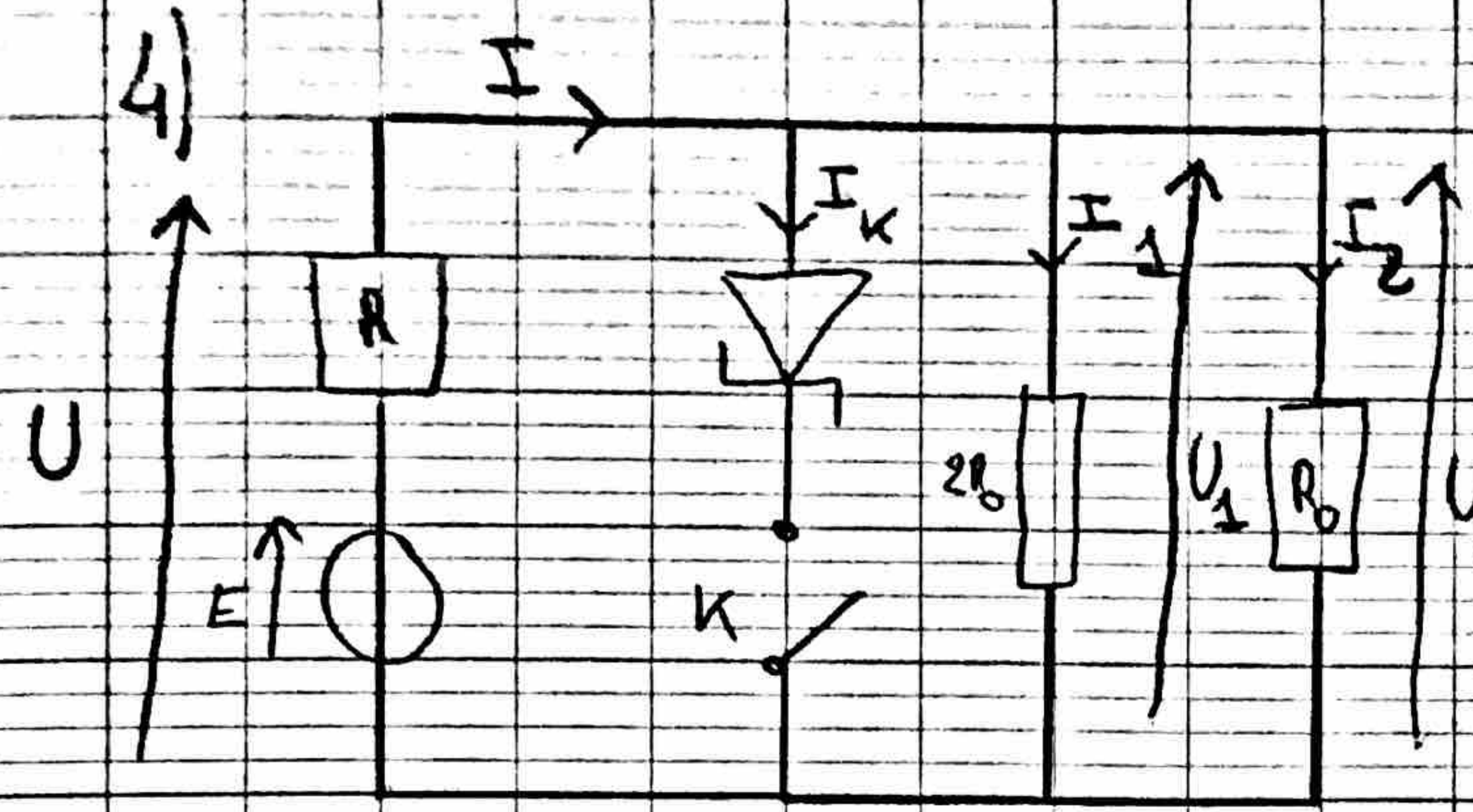
The new operating points are  $I = 10mA$  and  $U = 1V$

(Once again, in this method the uncertainties are higher than with a direct calculus). Yes indeed.

BONUS: +0.25

Very good comments and justifications plus all equations spec

0.25



When K is open there is no intensity in the branch so  $I_k = 0$   
 We can even remove it from the circuit.

Then thanks to Kirchhoff's current law (KCL) we know that  $I = I_1 + I_2$  (1)

Moreover in PSC we know that  $I = 0,03 - \frac{U}{50}$  (2) *Do not mix numerical values with literal expressions. Keep the latter one!*

From Kirchhoff's voltage law (KVL) we have  $U = U_1 = U_2$  (3) and in PSC  $U_1 = 2R_0 I_1$  (4) and  $U_2 = R_0 I_2$  (5)

Since  $U_1 = U_2$  (3) we have  $2R_0 I_1 = R_0 I_2$  (4) & (5) hence  $I_1 = \frac{I_2}{2}$  *Non homogeneous expression!!*

From (1) we have  $I = \frac{I_2}{2} + I_2 = \dots$

I did not manage to finish these 2 questions because of time but the method is the same for both (except that for the 5th question we need to take  $i_k$  into account. Yes so the method won't be the same at the end.

Method question 4 and 5

I first need to draw a scheme and define all the conventions.  
 Then thanks to KCL I can write the intensity in terms of other (I need 2 equations for 4 and 3 for 5th question) exactly.  
 Then with KVL I obtain other equation and I can then solve a system to find all the intensities.

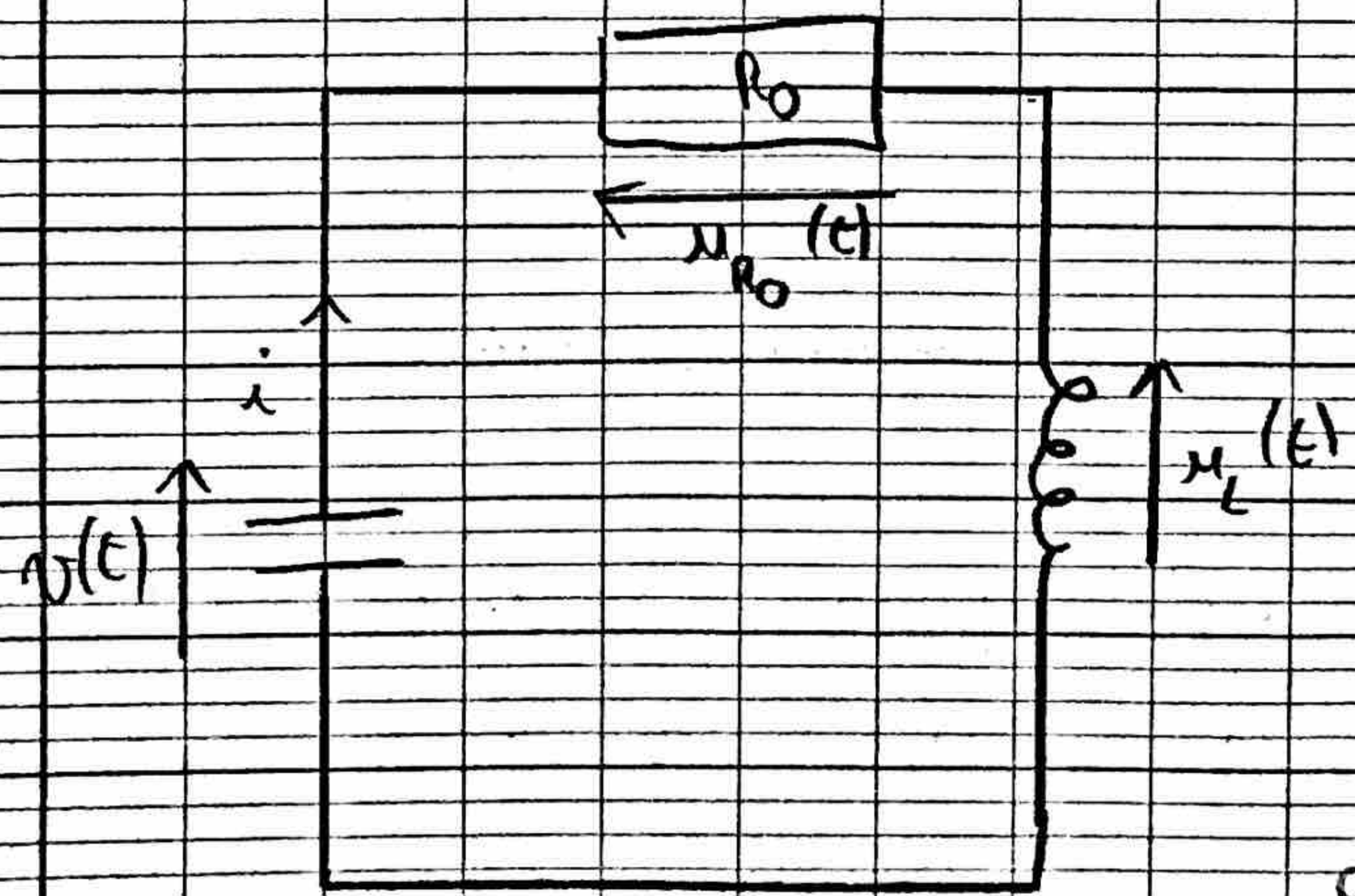
Yes, this is indeed the method you should have used for this question 4. (2)

specified.

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Assignment 2

1) For  $t > 0$  we have this circuit (with the capacitor charged).



From KVL we have

$$v(t) = u_{R_0}(t) + u_L(t) \quad (1)$$

with  $i(t) = -C \frac{dv}{dt}$  (2)

and  $u_L(t) = L \frac{di}{dt}$  (3)

and  $u_{R_0} = i(t) \times R_0$  (4)

No here this is ASC! PSC

0.5

0.5

0.25

0.25

0.5 d'Arbie 2) From question 1 we have: from (1); (3); (4).

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$$v(t) = i(t) \cdot R_0 + L \frac{di}{dt} \Leftrightarrow i(t) \cdot R_0 + L \frac{di}{dt} - v(t) = 0$$

0.5 then from (2):  $-LC \frac{d^2 v}{dt^2} - CR_0 \frac{dv}{dt} - v(t) = 0$

$$\Leftrightarrow LC \frac{d^2 v}{dt^2} + CR_0 \frac{dv}{dt} + v(t) = 0 \quad *$$

0.5  $\Leftrightarrow \frac{d^2 v}{dt^2} + \frac{R_0}{L} \frac{dv}{dt} + \frac{1}{LC} v(t) = 0$

$$\Leftrightarrow \frac{d^2 v}{dt^2} + 2\delta \frac{dv}{dt} + \omega_0^2 v(t) = 0$$

0.5 with  $\delta = \frac{R_0}{2L}$  and  $\omega_0 = \frac{1}{\sqrt{LC}}$

\* This equation is Homogeneous because:  $\triangle$  discussion equation  $\neq$  equation.

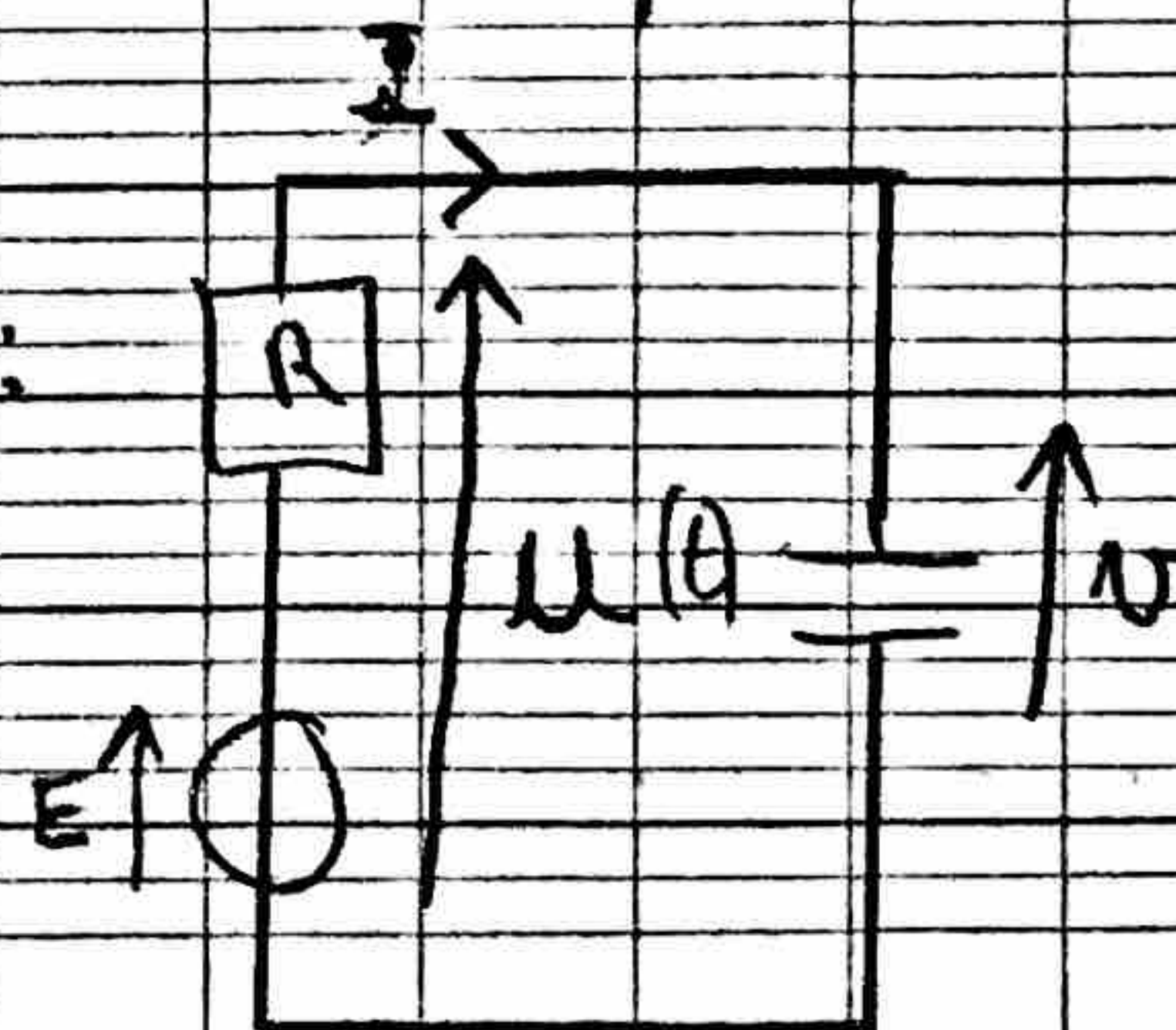
BONUS: +0.25  $\frac{1}{T^2} \times [v] + \frac{1}{T} \times [v] + [v] = 0$  the rest is only changed of writing. yes

But the constant I find feels weird. which constant? <sub>pse</sub>

3)  $v(t=0^+) = v(t=0^-) \stackrel{psc}{=} u(t) = E - R_0 i(t)$  Yes

$\hookrightarrow$  voltage across a capacitor is constant as a function of time

at time  $t < 0$ :



0.25

Q.25  $i(t=0^+) = i(t=0^-) = 0$  / since  $u(t) = i(t)R$

↳ continuous function of time /

we have

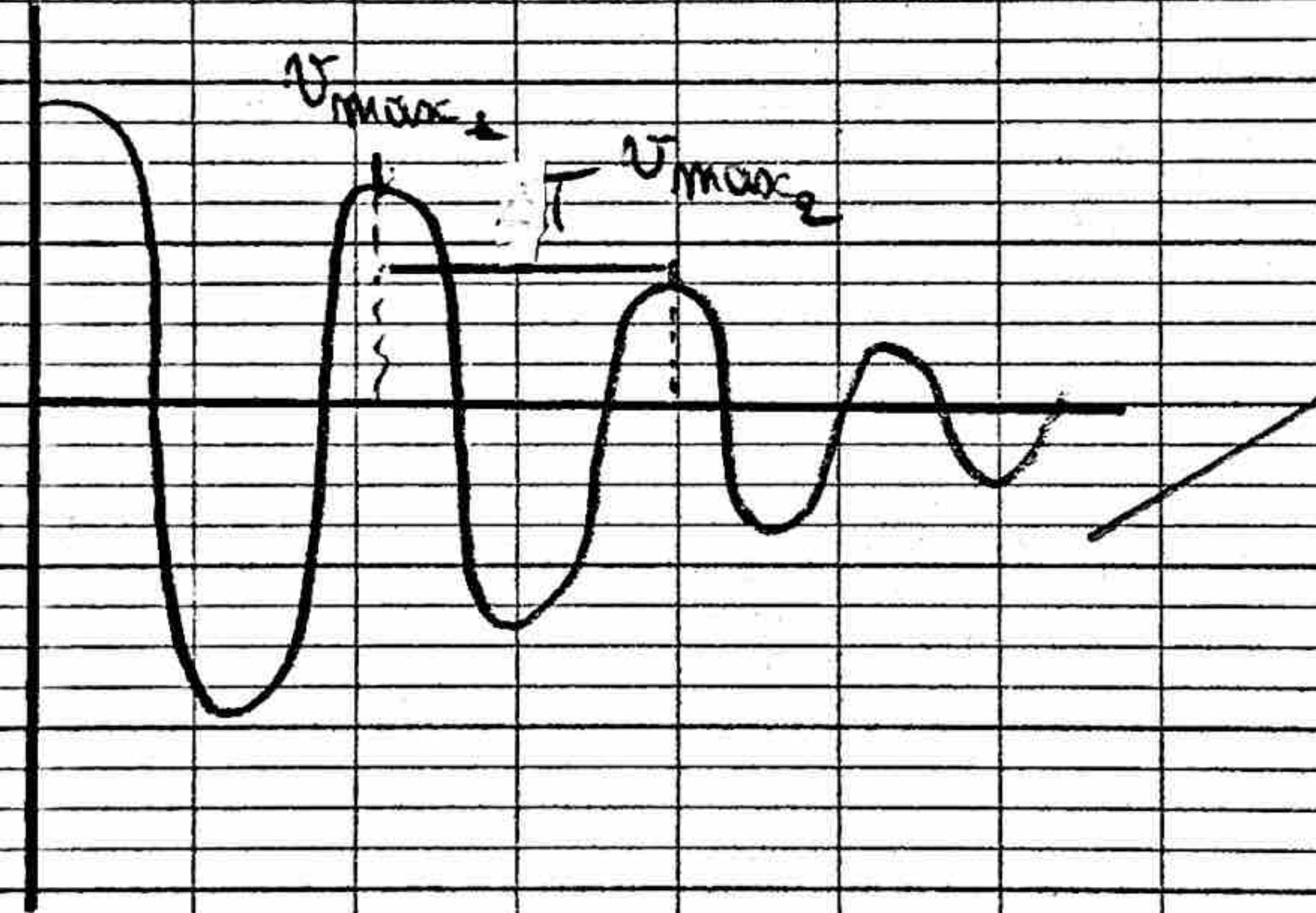
$u(t=0^+) = u(t=0^-) = 0$  X

↳ continuous function of time

$u_L(t=0^+) = u_L(t=0^-) = 0$  / since at  $t < 0$  switch was open.

↳ voltage across a coil is a continuous function of time. Noooo! For a coil, this is the intensity, which is a continuous function of  $t$ .

4) We know that a pseudo period corresponds to  $\frac{1}{2}T$  as shown below:



Q.5 Graphically we obtained  $T = 70 \mu s$  /

But we have different sources of uncertainties (random and systematic):

↳ uncertainties on the position of  $\frac{1}{2}$  max (estimated at  $2 \mu s \times 2$ )

↳ uncertainty on the ruler (estimated at  $1 \mu s \times 2$ )

Hence  $\Delta T = 6 \mu s$  /

Q.5

Hence  $T = (70 \pm 6) \mu s$  (High uncertainty due to graphic method).

5) Graphically  $A = ?$

$\phi = ?$

6)  $T \approx \frac{2\pi}{\omega_0} \Leftrightarrow \omega_0 = \frac{2\pi}{T} = 89759 \text{ Umst?}$

Never give a numerical result without its uncertainty.

We know from question 2) (if it is correct) that:

0.25  $\omega_0 = \frac{1}{\sqrt{LC}} \Leftrightarrow L = \frac{1}{\omega_0^2 \times C}$

0.25 (method)  $L_{\max} = \frac{1}{\omega_0^2 \times C_{\min}} = \frac{1}{\omega_0^2 \times (C - \Delta C)} = 0,0137 \text{ H}$

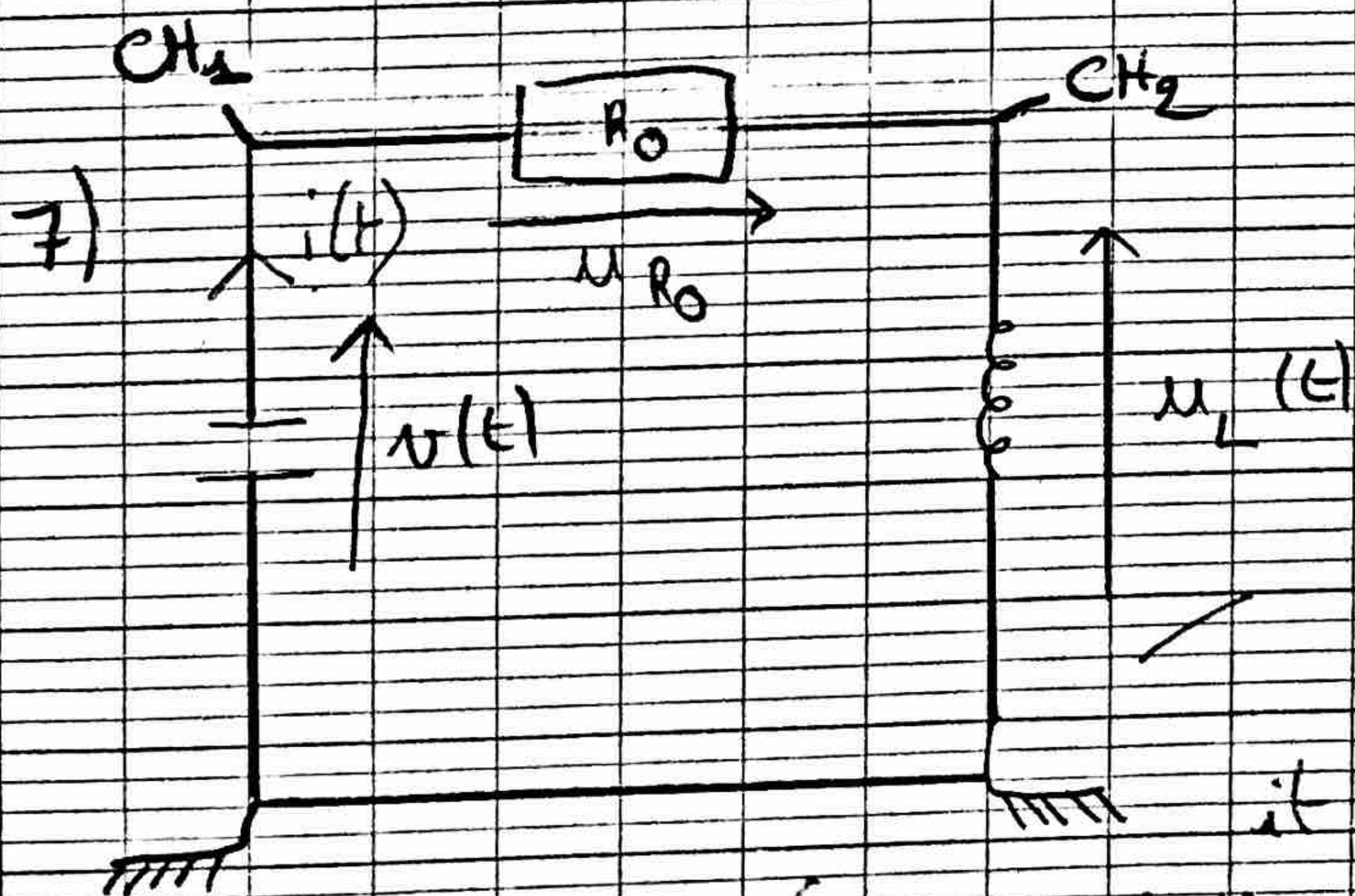
this can also be minor max.

0.25/0.5  $L_{\min} = \frac{1}{\omega_0^2 \times C_{\max}} = \frac{1}{\omega_0^2 \times (C + \Delta C)} = 0,0113 \text{ H}$

$L = \frac{L_{\max} + L_{\min}}{2} = 0,0125 \text{ Umst?}$

$\Delta L = \frac{|L_{\max} - L_{\min}|}{2} = 1,2 \cdot 10^{-3} \text{ Umst?}$  (Uncertainty is a bit higher because the equation used at the beginning is not a perfect one)

0.25  $L = (11,3 \pm 1,2) \text{ mH}$



We can visualize  $v(t)$  directly in Channel 1.

As for  $i(t)$  we can visualize it through the math function (careful at the scale used) by doing  $CH_2 - CH_1$

0.25/0.5

we would obtain the signal corresponding to

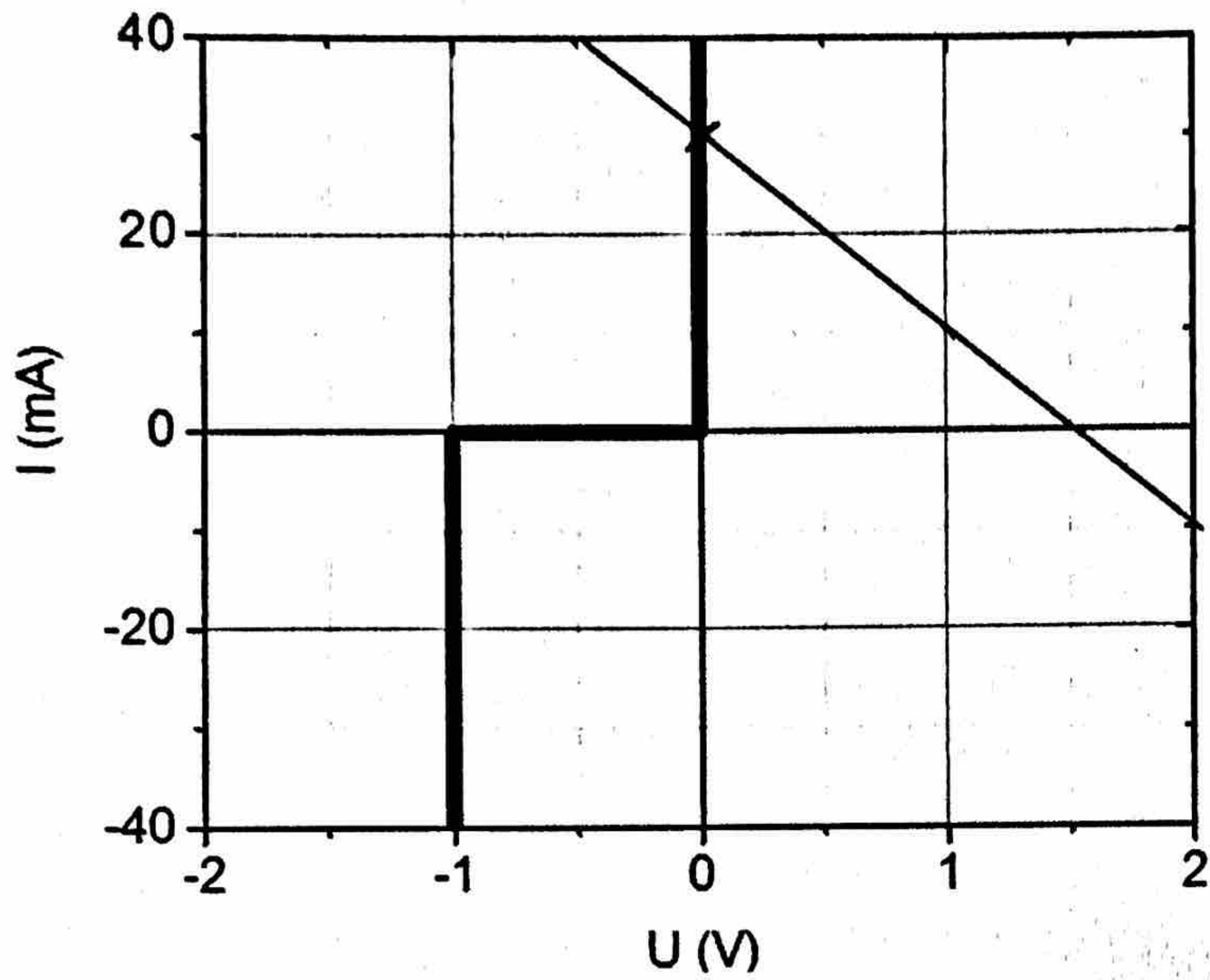
$u_{R_0} = i(t) R_0$

You have to do  $CH_1 - CH_2$  to get  $+i R_0$ !

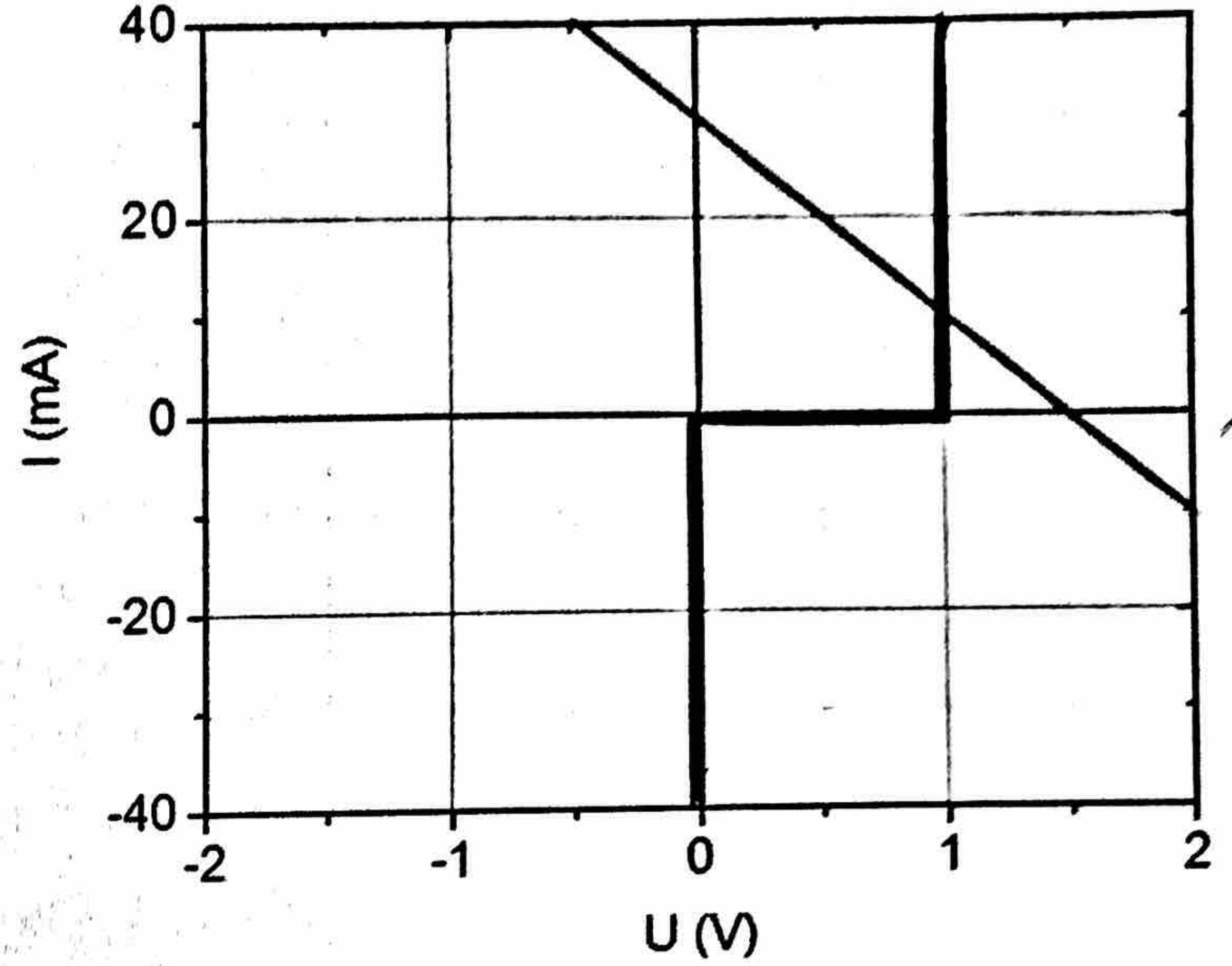
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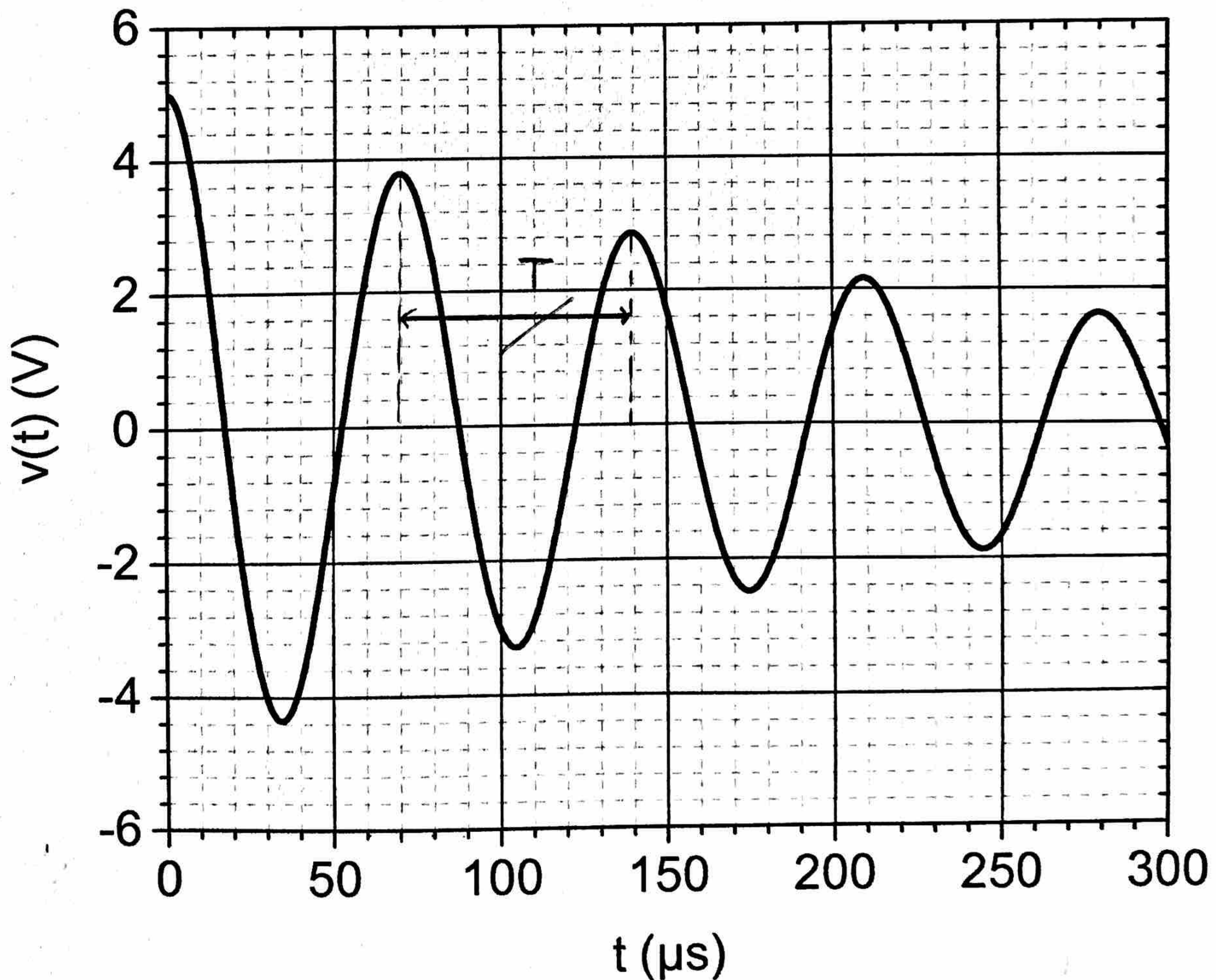
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Appendix 1: I-V curve of a Zener diode in passive sign convention



Appendix 2



Appendix 3