

1 – Prisms placed side by side (6 points)

1. $N \sin \alpha = n \sin \beta$	0.5
2. $\beta = \frac{\pi}{2} - \gamma$	0.5
2. At I_2 : The critical angle is such that $n \cdot \sin(i_c) = 1$, i.e. $\sin i_c = \frac{1}{n}$ Therefore we have $\sin \gamma > \frac{1}{n}$ At I_1 : $N \sin \alpha = n \sin \beta = n \sin(\frac{\pi}{2} - \gamma) = n \cos \gamma$ As a consequence, $N \sin \alpha < n \sqrt{1 - (\frac{1}{n})^2}$ Since $\alpha = 45^\circ$, we get $N < \frac{2}{\sqrt{2}} \sqrt{n^2 - 1}$	1 1 0.5 1 0.5
4. If $\varepsilon = 0$, $\delta = 0$ so $\gamma = 45^\circ$ and $\beta = 45^\circ$. By using the Snell-Descartes' law at I_1 , we get $N = n$	0.5 0.5

2 – Projection system (7 points)

1. real object (we can touch the document), real image (observed on a screen)	0.25 + 0.25
2. converging lens with the object placed before F	0.5 + 0.5
3. We have 3 equations with 3 unknown elements: I : $\frac{1}{f'} = \frac{1}{OA'} - \frac{1}{OA}$, which gives $f' = \frac{OA' \cdot OA}{OA - OA'}$ II : $\gamma = \frac{A'B'}{AB} = \frac{OA'}{OA}$, i.e. $OA' = \gamma \cdot OA$ III : $D = AO + OA' = -OA + OA'$, By combining II & III, we get $OA = \frac{D}{\gamma - 1}$ and $OA' = \frac{\gamma D}{\gamma - 1}$ Then, from I, $f' = \frac{-\gamma}{(\gamma - 1)^2} D$	0.5 0.5 0.5 1 + 1 1
4. $\gamma = -9$ $f' = 9 \text{ cm}$	0.5 0.5 (0 if no unit)

3 – Ray-tracing (3 points)

	1
	1 + 1

4 – Image-object ray diagrams (4 points)

	<p>2 + 2</p> <p>0.5 for each ray</p> <p>0.5 for the object</p> <p>0 if rays and construction lines cannot be distinguished from each other</p>
--	---