

Thermodynamics

Test May 17th 2024

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	Please enter you student number, and write your name above.
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Duration: 2 h - All booklets, notes and calculators authorised - No computer or tablet, no wifi no 4/5G

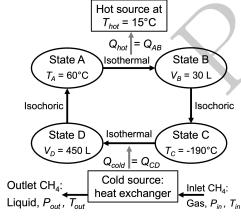
Methane (CH₄): thermodynamic data

Molar mass : $M_{\rm CH_4} = 16 \, \rm g/mol$

Gaseous molar specific heat at constant volume : $\bar{C}_{V_m(\text{CH}_4)} = 27.4 \,\text{J/(mol K)}$ Gaseous molar specific heat at constant pressure : $\bar{C}_{P_m(\text{CH}_4)} = 35.8 \,\text{J/(mol K)}$

Latent heat at $T_{\text{vap}} = -162\,^{\circ}\text{C}$: $L_{\text{vap(CH_4)}} = 511\,\text{kJ/kg}$ Saturating vapor pressure at $T_{\text{vap}} = -162\,^{\circ}\text{C}$: $P_{\text{CH_4}}^* = 1\,\text{bar}$

1 The Stirling cryogenerator (15 points)



The Stirling cryogenerator is a refrigerator device allowing the obtention of liquid methane. It is made by a closed piston-cylinder that does not exchange shaft work and it contains an amount of moles of helium (He, an **ideal monoatomic gas**) equal to $n_{\rm He}=265\,{\rm mol}$. Its working principle is based on the Stirling cycle made of the four reversible processes represented in the side figure. By using the data available in the exercise and the tutorial booklet, and by clearly explicating your reasoning:

Question 1 What is the numerical value of P_B (in bar)?

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Give and demonstrate the literal expression of the heat Q_{hot} exchanged in the process Question 2 $A \to B$ as function of the available data. Empty Question 3 What is the numerical value of Q_{hot} in MJ? Give and demonstrate the literal expression of the heat Q_{BC} exchanged in the process Question 4 $B \to C$ as function of the available data. Empty Question 5 What is the numerical value of Q_{BC} in MJ? Give the literal expression of the CoP as function of the available data. Question 6 0 Empty 3

Pour votre examen, imprimez de préférence les documents compilés à l'aide de auto-multiple-choice.

Question 7 Give the numerical value	ne of CoP (attention : $CoP_{ref} \ge 0$, not 1).		
	4 <u>5</u> 6 <u>7</u> 8 <u>9</u>		
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Let's focus now on the cold source. It is a heat exchanger (open system) where heat is obtained by a stream of methane $\dot{m}_{\text{CH}_4} = 34.5 \text{kg/s}$ at $P_{in} = P_{out} = 1 \text{bar}$ entering the exchanger in the gaseous state at T_{in} and leaving it as saturated liquid ¹ at $T_{out} = -162 ^{\circ}\text{C}$.			
Question 8 Considering that the rate of heat lost by the methane stream is $\dot{Q}_{\text{CH}_4} = -25 \text{MW}$, give and demonstrate the literal expression of T_{in} as function of the available data.			
Question 9 What is the	numerical value of T_{in} in °C?		
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The Stirling Cycle in practice	Q		
A Striling cryogenerator is made of two pistons moving independently (piston "P ₁ " and "P ₂ "). The working gas (He) lies in a chamber represented in black on the figure. He gas can circulate around P ₂ but not P ₁ . On the figure, are represented the four stages of the Stirling cooling cycle, but the order is lost. Can you re-order them and tell which scheme corresponds to which state?			
Question 10 State A:	Question 12 State C:		
Question 11 State B:	Question 13 State D:		
	II III IV		
1. Saturated liquid: a liquid that is about to vaporise (vapour and liquid are at equilibrium).			

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2 Water lost during breathing (5 pts)

Question 14 How much water is lost by human body due to breathing in dry air during a day (give the result as a mass proportion of beverage water intake)?

Indications : The average tidal volume of human lungs (volume of air moved into or out of the lungs in 1 breath) is $0.5 \, \text{L}$. The average beverage water intake is $1.5 \, \text{L}$ per day.

