## Thermodynamics


$\longleftarrow \quad$ Please enter you student number, and write your name above.

NAME, First Name :
$\qquad$
$\qquad$

Duration : 2 h - All booklets, notes and calculators authorised - No computer or tablet, no wifi no 4/5G

## Methane $\left(\mathrm{CH}_{4}\right)$ : thermodynamic data

Molar mass : $M_{\mathrm{CH}_{4}}=16 \mathrm{~g} / \mathrm{mol}$
Gaseous molar specific heat at constant volume : $\bar{C}_{V_{m}\left(\mathrm{CH}_{4}\right)}=27.4 \mathrm{~J} /(\mathrm{mol} \mathrm{K})$
Gaseous molar specific heat at constant pressure : $\bar{C}_{P_{m}\left(\mathrm{CH}_{4}\right)}=35.8 \mathrm{~J} /(\mathrm{mol} \mathrm{K})$
Latent heat at $T_{\text {vap }}=-162^{\circ} \mathrm{C}: L_{\text {vap }\left(\mathrm{CH}_{4}\right)}=511 \mathrm{~kJ} / \mathrm{kg}$
Saturating vapor pressure at $T_{\text {vap }}=-162^{\circ} \mathrm{C}: P_{\mathrm{CH}_{4}}^{*}=1$ bar

## 1 The Stirling cryogenerator (15 points)



The Stirling cryogenerator is a refrigerator device allowing the obtention of liquid methane. It is made by a closed piston-cylinder that does not exchange shaft work and it contains an amount of moles of helium (He, an ideal monoatomic gas) equal to $n_{\mathrm{He}}=265 \mathrm{~mol}$. Its working principle is based on the Stirling cycle made of the four reversible processes represented in the side figure. By using the data available in the exercise and the tutorial booklet, and by clearly explicating your reasoning :

Question 1 What is the numerical value of $P_{B}$ (in bar)?


Question 2 Give and demonstrate the literal expression of the heat $Q_{h o t}$ exchanged in the process $A \rightarrow B$ as function of the available data.
$\square$ Empty $\square 0 \square 1 \square 2 \square 3 \square 4$

Question 3 What is the numerical value of $Q_{h o t}$ in MJ?


Question 4 Give and demonstrate the literal expression of the heat $Q_{B C}$ exchanged in the process $B \rightarrow C$ as function of the available data.
$\square$ Empty $\square 0 \square 1 \square 2 \square 3 \square_{4}$

Question 5 What is the numerical value of $Q_{B C}$ in MJ?


Question 6 Give the literal expression of the $C o P$ as function of the available data.

Question 7 Give the numerical value of $C o P$ (attention: $C o P_{\text {ref }} \geq 0$, not 1).
$\square 0 \square 1 \square 2 \square 3 \square 4 \square 5 \square 6 \square 7 \square 8 \square 9$

0 $\square$ $\square$ $\qquad$ $\square 4$ $\square 5$ $\square 6$ $\square$ 7 $\square$ 8 $\square$
$\qquad$ $\square 2$ $\square 3$ $\square 4$ $\square 5$ $\square 6$ $\qquad$ 7 $8 \square 9$

Let's focus now on the cold source. It is a heat exchanger (open system) where heat is obtained by a stream of methane $\dot{m}_{\mathrm{CH}_{4}}=34.5 \mathrm{~kg} / \mathrm{s}$ at $P_{\text {in }}=P_{\text {out }}=1$ bar entering the exchanger in the gaseous state at $T_{\text {in }}$ and leaving it as saturated liquid ${ }^{1}$ at $T_{\text {out }}=-162^{\circ} \mathrm{C}$.
Question 8 Considering that the rate of heat lost by the methane stream is $\dot{Q}_{\mathrm{CH}_{4}}=-25 \mathrm{MW}$, give and demonstrate the literal expression of $T_{i n}$ as function of the available data.
$\square$ Empty $\square_{0} \square_{1} \square_{2} \square_{3} \square_{4}$

Question $9 \quad$ What is the numerical value of $T_{\text {in }}$ in ${ }^{\circ} \mathrm{C}$ ?

$\square$ $\square 2 \square 3$ $\square$ $\square 5$
$\square 5$ $\square 6$
$\square 6$ $\qquad$ $7 \square 8$
$7 \square 8$ $\square 9$
$\square 9$

## The Stirling Cycle in practice

A Striling cryogenerator is made of two pistons moving independently (piston " $\mathrm{P}_{1}$ " and " $\mathrm{P}_{2}$ "). The working gas (He) lies in a chamber represented in black on the figure. He gas can circulate around $\mathrm{P}_{2}$ but not $P_{1}$. On the figure, are represented the four stages of the Stirling cooling cycle, but the order is lost.

Can you re-order them and tell which scheme corresponds to which state?


Question 10 State A :
Question 12 State C :
$\square$ IV $\quad \square$ III $\quad \square$ II
$\square$ I $\square$ II $\square$ I $\square \mathrm{IV}$
$\square$ III
Question 11 State B :
Question 13 State D :


1. Saturated liquid : a liquid that is about to vaporise (vapour and liquid are at equilibrium).

Pour votre examen, imprimez de préférence les documents compilés à l'aide de auto-multiple-choice.

## 2 Water lost during breathing (5 pts)

Question 14 How much water is lost by human body due to breathing in dry air during a day (give the result as a mass proportion of beverage water intake)?
Indications : The average tidal volume of human lungs (volume of air moved into or out of the lungs in 1 breath) is 0.5 L . The average beverage water intake is 1.5 L per day.

Vide Faux $\square$ 1 $\square$ 3 4 $6 \square 7$ 10

